

Note: Pre-Lab 4 is also due next Monday. You should be able to do it, now.

1.a) Determine the type number of the following open-loop Z-domain transfer functions:

$$i) G(z) = \frac{10(z+1)^2}{z(z-1)} \quad ii) G(z) = \frac{10(z+1)^3}{z^2(z-1)} \quad iii) G(z) = \frac{10(z+1)^3}{z(z-1)^2}$$

b) Let  $T_s=100$  msec and find the static error coefficients  $K_p$ ,  $K_v$  and  $K_a$  for problem 1a) (assume unity feedback).

c) For each of the closed-loop unity feedback systems in part a), find:

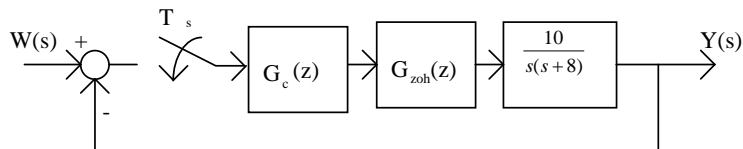
i)  $e_{ss}$  due to a step

ii)  $e_{ss}$  due to a ramp

iii)  $e_{ss}$  due to a parabola

d) Sketch the root locus for the systems in part a).

2. Given the system



a) Find a Z-domain model for the open-loop system including the ZOH if  $T_s = 10$  msec.

b) What type number is your Z-domain model? What type is the original model?

c) Find  $e_{ss}$  due to a step,  $e_{ss}$  due to a ramp, and  $e_{ss}$  due to a parabola for your uncompensated Z-domain model.

d) Given the following transient specifications:  $t_s < 0.4$  sec and  $M_p < 2\%$ . Illustrate the region of the s-plane and the z-plane where we must place our dominant poles to satisfy these specs.

e) Design  $G_c(z)$  (plus possibly a lag compensator) to meet the above specs plus the added spec that  $e_{ss}$  due to ramp  $\leq 1/50$ .

f) Simulate a step and ramp response of your closed-loop compensated digital system using `dlsim()` in MATLAB. Measure  $t_s$ ,  $M_p$ , and  $e_{ss}$  (both step and ramp).

g) How do your digital compensator numbers compare to the  $G_c(z)$  we designed for this system in HWs #16 and #17?